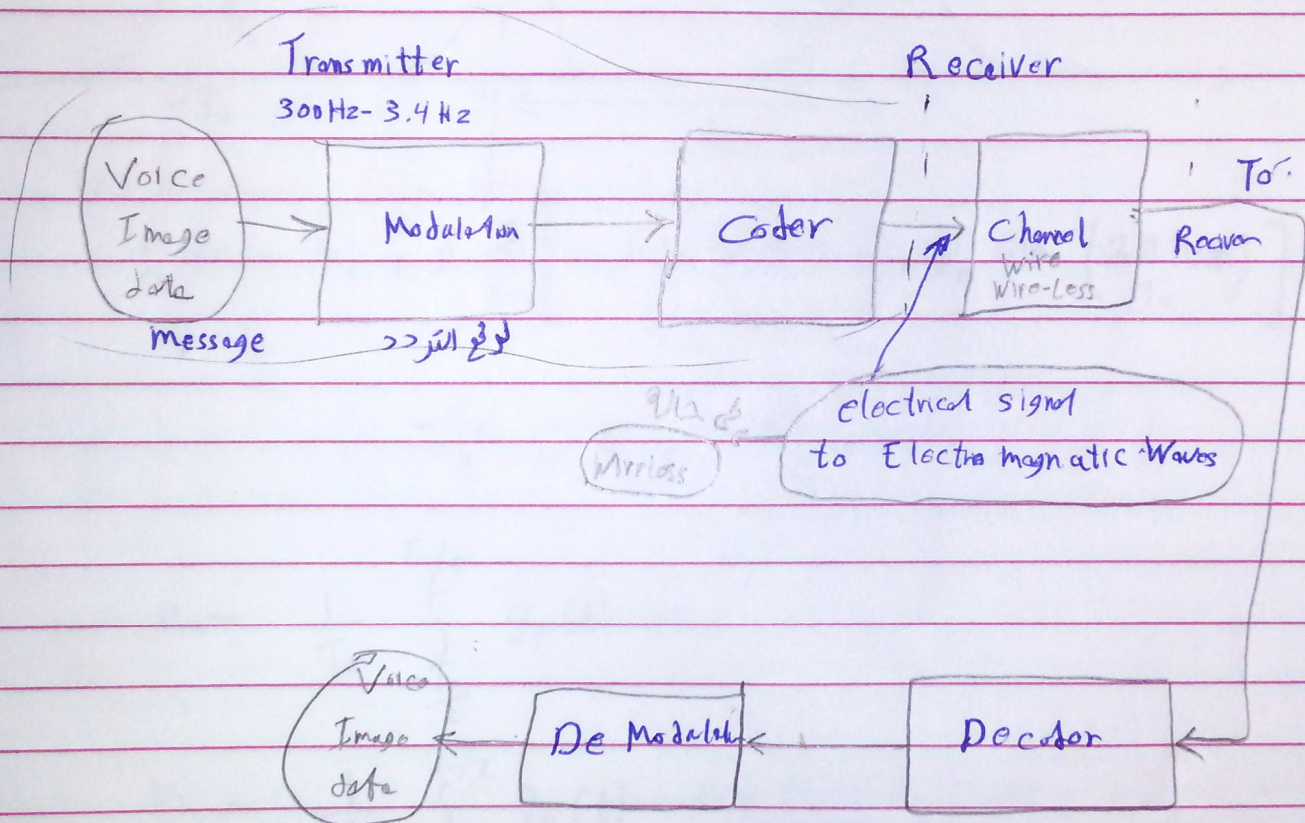


Communication Systems

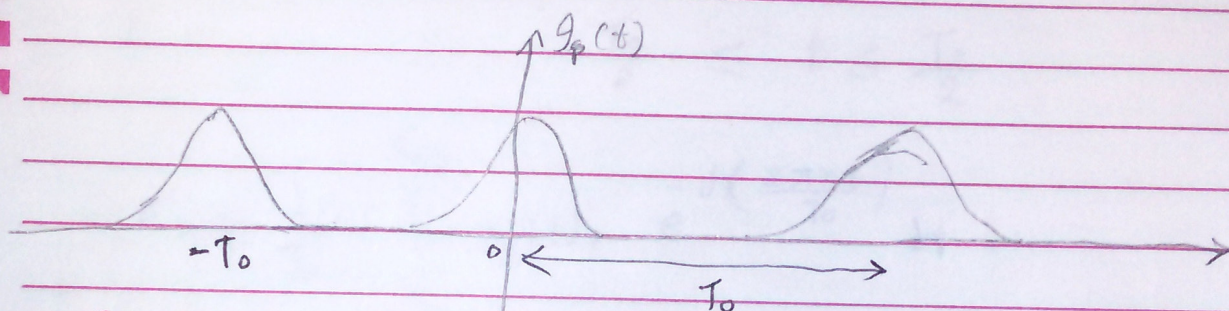
- ① Signal and Systems
- ② Amplitude Modulation (AM)
- ③ Angle Modulation (PM, FM)
- ④ Transmission Media



Chapter 1 : Signals and systems

(I) Fourier Series:

Sine, Cosine etc. are Periodic signal \Rightarrow $\sin(\omega t)$ \Rightarrow $\cos(\omega t)$ -



Trig geometric Fourier series

$$g_p(t) = a_0 + 2 \sum_{n=1}^{\infty} \left[a_n \cos\left(\frac{2\pi n}{T_0} t\right) + b_n \sin\left(\frac{2\pi n}{T_0} t\right) \right]$$

$$-\frac{T_0}{2} \leq t \leq \frac{T_0}{2}$$

$$a_0 = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} g_p(t) \cdot dt$$

$$a_n = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} g_p(t) \cdot \cos\left(\frac{2\pi n t}{T_0}\right) dt$$

$$b_n = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} g_p(t) \cdot \sin\left(\frac{2\pi n t}{T_0}\right) dt$$

even $\Rightarrow a_n = \checkmark \quad b_n = 0$

odd $\Rightarrow a_n = 0 \quad b_n = \checkmark$

Exponential Fourier Series :

$$g_p(t) = \sum_{n=-\infty}^{\infty} K_n e^{j \frac{2\pi n t}{T_0}}$$

$$-\frac{T_0}{2} \leq t \leq \frac{T_0}{2}$$

$$C_n = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} g_p(t) \cdot e^{-j \left(\frac{2\pi n t}{T_0} \right)} dt$$

Dirichlets Condition:

دالة في فترة معينة
Fourier series

① The Function $g_p(t)$ has single valued within T_0

② Integrable absolutely $\int_{-T_0/2}^{T_0/2} |g_p(t)| dt < \infty$

③ $g_p(t)$ has a finite number of maximum and minimum

$$R=1.2$$

القيمة المتوسطة في فترة T_0

Fourier series

متوسط
القيمة

$$P_{avg} = \sum_{n=-\infty}^{\infty} |C_n|^2$$

Parseval's
theorem

$$P = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} |g_p(t)|^2 dt$$

القيمة

$$g_p(t) = \sum_{n=-\infty}^{\infty} C_n e^{j \frac{2\pi n t}{T_0}}$$

$$|g_p(t)|^2 = g_p(t) \cdot g_p^*(t)$$

$$P = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} g_p^*(t) \cdot \sum_{n=-\infty}^{\infty} C_n e^{j \frac{2\pi n t}{T_0}} dt$$

$$P = \frac{1}{T_0} \sum_{n=-\infty}^{\infty} C_n \int_{-T_0/2}^{T_0/2} g_p^*(t) \cdot e^{j \frac{2\pi n t}{T_0}} dt$$

$$C_n = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} g_p(t) e^{-j \frac{2\pi n t}{T_0}} dt$$

$$C_n^* = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} g_p^*(t) e^{j \frac{2\pi n t}{T_0}} dt$$

$$P = \sum_{n=-\infty}^{\infty} C_n \cdot C_n^*$$

$$P = \sum_{n=-\infty}^{\infty} |C_n|^2$$

~~✗~~

استعملنا دالة الجهد

إذا $g_p(t) \rightarrow$ جهد

$$P = \frac{P}{R}$$

$g_p(t) \rightarrow$ الجهد

$$P = P \cdot R$$